

# AI Foundation Models Facilitate Real-time Global GNSS Precipitable Water Vapor Retrieval with Sub-millimeter Accuracy

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## Abstract

Currently, over 20,000 Global Navigation Satellite Systems (GNSS) stations are installed worldwide to provide tropospheric delay products with high-quality and high temporal resolution (5 min). However, few of these stations are equipped with on-site meteorological sensors, leading to the challenge of the real-time transformation of this tropospheric delay into accurate precipitable water vapor (PWV). We propose a real-time high-accuracy GNSS PWV retrieval method based on artificial intelligence weather forecast foundation models. This innovative approach efficiently calculates integral zenith hydrostatic delay (ZHD) and integral weighted mean temperature (T<sub>m</sub>) at any global location locally within seconds, bypassing inaccuracies inherent in empirical ZHD and T<sub>m</sub> models, significantly reducing PWV errors. The method is evaluated on three representative foundation models, Pangu-Weather, GraphCast, and FengWu, showing precision loss of PWV below 0.1 mm using 6-hour forecasts. It offers a robust solution for instantaneous GNSS PWV retrieval and enhances global hazardous weather monitoring and alert systems.

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## Key Points:

- Proposes real-time GNSS PWV retrieval method based on weather forecast foundation models represented by Pangu-Weather, GraphCast and FengWu
- Generates integral ZHD and Tm at any global position locally within seconds, circumventing inaccuracies inherent in empirical ZHD and Tm models
- On a global scale, the PWV error introduced by ZHD and Tm using the 6-hour forecast under the new method is less than 0.1 mm

## Abstract

Currently, over 20,000 Global Navigation Satellite Systems (GNSS) stations are installed worldwide to provide tropospheric delay products with high-quality and high temporal resolution (5 min). However, few of these stations are equipped with on-site meteorological sensors, leading to the challenge of the real-time transformation of this tropospheric delay into accurate precipitable water

30 vapor (PWV). We propose a real-time high-accuracy GNSS PWV retrieval method based on artificial  
31 intelligence weather forecast foundation models. This innovative approach efficiently calculates  
32 integral zenith hydrostatic delay (ZHD) and integral weighted mean temperature ( $T_m$ ) at any global  
33 location locally within seconds, bypassing inaccuracies inherent in empirical ZHD and  $T_m$  models,  
34 significantly reducing PWV errors. The method is evaluated on three representative foundation models,  
35 Pangu-Weather, GraphCast, and FengWu, showing precision loss of PWV below 0.1 mm using 6-hour  
36 forecasts. It offers a robust solution for instantaneous GNSS PWV retrieval and enhances global  
37 hazardous weather monitoring and alert systems.

38

### 39 **Plain Language Summary**

40 The tropospheric delay products can be provided at over 20,000 Global Navigation Satellite Systems  
41 (GNSS) stations worldwide. The products can be converted into highly accurate and high-quality  
42 precipitable water vapor (PWV), which is crucial for understanding global water and energy cycles, as  
43 well as for meteorological and climatic studies. However, the conversion of GNSS zenith total delay  
44 (ZTD) into PWV relies on two key factors: zenith hydrostatic delay (ZHD) and weighted mean  
45 temperature ( $T_m$ ), typically provided by co-located radiosondes. Unfortunately, the majority of GNSS  
46 stations do not meet this requirement. Recent progress in artificial intelligence (AI) provides us new  
47 opportunities to address this challenge. We propose a real-time GNSS PWV retrieval method based on  
48 AI weather forecast foundation models (i.e. Pangu-Weather, GraphCast, and FengWu), from which  
49 ZHD and  $T_m$  are obtained to transform GNSS ZTD into PWV. This approach effectively avoids  
50 introducing empirical model errors into the PWV by locally generating forecasted integrated ZHD and  
51  $T_m$  for any global location within seconds. The PWV error introduced using 6-hour forecast results is  
52 less than 0.1 mm. This study offers a crucial solution for real-time GNSS PWV inversion, which will  
53 be valuable for monitoring and providing early warnings of meteorological hazards worldwide.

54

### 55 **1. Introduction**

56 Precipitable water vapor (PWV) is the primary greenhouse gas and an integral part of the climate and  
57 weather system, influencing the global water and energy cycles (*Rocken et al., 1997; Wang et al., 2007;*  
58 *Adams et al., 2023; Ding et al., 2022a*). The transport and dissipation of PWV are affected by several  
59 ecological and meteorological factors such as vegetation cover, topography (*Yu et al., 2017*), drought

60 (*Wang et al., 2018*) and temperature (*Ma et al., 2022*), which leads to its high variability in time and  
61 space (*Jiang et al., 2024*). Accurate PWV measurements have been a major challenge (*Zheng et al.,*  
62 *2022*). The derivation of PWV from Global Navigation Satellite Systems (GNSS) stands out as an  
63 increasingly promising approach due to its low cost, high temporal resolution, all-weather  
64 observational capability (*Ding et al., 2017; Miranda et al., 2023*), and the consistent delivery of PWV  
65 with high accuracy and data integrity (*Vaquero-Martínez et al., 2019; Ding et al., 2022b*). GNSS-  
66 driven PWVs have been widely used for monitoring and prediction of hurricane tracks (*Ejigu et al.,*  
67 *2021*), responding to thermal anomalies after the earthquake (*Guo et al., 2023*), forecasting and  
68 monitoring heavy rainfall (*Huang et al., 2021; Zhao et al., 2020*) and unveiling the characteristics of  
69 extreme drought and wetness events (*Zhu et al., 2024*).

70 However, the PWV could not be obtained directly by GNSS measurements. It can be estimated  
71 through two steps: (1) the zenith hydrostatic delay (ZHD) is subtracted from the zenith total delay  
72 (ZTD) to obtain a clean zenith wet delay (ZWD); and (2) the ZWD is converted to PWV by multiplying  
73 it by a conversion factor, which is determined by the weighted average temperature ( $T_m$ ). Therefore,  
74 the PWV error is affected by the ZHD and  $T_m$  errors. The incorrect ZHD and  $T_m$  will lead to PWV  
75 errors of several millimeters (*Yuan et al., 2014; Li et al., 2018; Ding et al., 2023*) and may lead to  
76 negative computed GNSS PWVs at high altitudes where water vapor is thin, as well as in polar regions  
77 (*Yuan et al., 2023*). Furthermore, the great majority of GNSS stations are not equipped with  
78 meteorological sensors, and even those that have sensors can only gather data from the surface, which  
79 is insufficient to meet the requirements of the vertical integration method for determining ZHD and  
80  $T_m$  in real time. As a result, they are forced to use an empirical model, which absorbs the PWV in the  
81 empirical model error, to settle for less-than-ideal results. *Zheng et al., (2022)* attempted to replace the  
82 ZTD to PWV transformation by machine learning, and they obtained better results than the traditional  
83 empirical model (using ERA5 as a reference, the RMSE of PWV decreased from 2.8 mm in the GPT3  
84 results to 2.4 mm). However, it is still actually an empirical model, which accuracy improvement may  
85 not satisfy the need for high-accuracy water vapor monitoring and acquisition. Therefore, in the  
86 traditional method, either post-processing is used to obtain meteorological data by reanalyzed data for  
87 GNSS PWV computation, or GNSS stations are co-located with radiosonde sites to obtain the  
88 atmospheric vertical profile data for GNSS PWV retrieval. The former cannot be done in real-time,  
89 and the latter is nearly impossible to achieve for special environments, such as shipboard GNSS PWV

90 retrieval at sea (*Wang et al., 2019; Wei et al., 2023; Wu et al., 2023*). Furthermore, traditional NWM  
 91 (Numerical Weather Model) forecasts (such as ECMWF IFS, NCEP GFS, etc.) can also help with real-  
 92 time GNSS PWV acquisition. Nevertheless, as this component normally requires authorization for  
 93 usage and depends on major meteorological agencies for generation and does not support local  
 94 inference, it is not included in the framework of this research.

95 In this contribution, we aim at providing high-accuracy and real-time GNSS PWV with global  
 96 coverage while minimizing the errors caused by inaccuracy ZHD and Tm. We present a new method  
 97 to acquire forecasted ZHD and Tm via AI weather forecast foundation models such as Pangu-Weather,  
 98 GraphCast and FengWu. By using this new method, empirical modeling errors can be minimized.  
 99 Notably, the computations can be performed on any user's local device, with global results achievable  
 100 within seconds. This paper is organized as follows. Section 2 describes GNSS tropospheric delay data  
 101 set and radiosonde data set, along with describing the method of converting GNSS ZTD to PWV.  
 102 Section 3 evaluates the performance of the proposed method. Section 4 summarizes and presents our  
 103 conclusions.

104

## 105 **2. Methods and Data**

106 The high-accuracy GNSS PWV depends on the high-accuracy ZHD and Tm parameters. In this study,  
 107 these parameters will be derived from AI weather forecast foundation models. In this section, we first  
 108 outline the streamlined computational process for real-time GNSS PWV retrieval. Then we introduce  
 109 three representative foundation models used in our experiments: Pangu-Weather, GraphCast, and  
 110 FengWu, and give the flowchart under this new method. Finally, the GNSS tropospheric products and  
 111 radiosonde data of 2022 that serve to assess the accuracy are described.

112

### 113 **2.1. PWV Retrieval from GNSS Tropospheric Delays**

114 The high-precision ZWD is first obtained by subtracting the high-precision ZHD from the GNSS ZTD  
 115 (*Jade et al., 2008*):

$$116 \quad ZWD = ZTD - ZHD \quad (1)$$

117 The ZHD is defined as the integral of the refractive index along the path in the zenith direction  
 118 and is calculated as follows:

$$119 \quad ZHD = 10^{-6} \int_{H_s}^{\infty} N_h(z) dz = \sum_{H_s}^{H_{top}} [(n_{h,i} - 1) \Delta H_i] \quad (2)$$

120 Where  $H_s$  and  $H_{top}$  are the height of the station (surface) and the top of the troposphere,  
 121 respectively. However, the calculation of the hydrostatic refraction index requires measurements of air  
 122 pressure and temperature in a vertical profile, which are difficult to obtain. A more common approach  
 123 is to compute the ZHD through the following Saastamoinen model (*Saastamoinen 1972*):

$$124 \quad ZHD = 2.2768 \cdot \frac{P_s}{1 - 2.66 \times 10^{-3} \cdot \cos(2\varphi_s) - 2.8 \times 10^{-7} h_s} \quad (3)$$

125 Where  $P_s$ ,  $\varphi_s$  and  $h_s$  are pressure, latitude and height of station locations. The Saastamoinen  
 126 model, requiring mainly surface pressure due to the fixed latitude and height at a station, delivers  
 127 millimeter-accurate ZHDs and is widely adopted for its simplicity and effectiveness.

128 After obtaining the ZWD, the GNSS PWV can be calculated by the following equations:

$$129 \quad PWV = \Pi \cdot ZWD \quad (4)$$

$$130 \quad \Pi = \frac{10^6}{R_w \cdot [k_2 - \varepsilon k_1 + k_3 / T_m]} \quad (5)$$

131 Where  $\Pi$  is the conversion factor, and  $\varepsilon = M_w / M_d$ ,  $R_w = R / M_w$  with the universal gas  
 132 constant  $R$ ;  $M_w$  and  $M_d$  are molar weight of water vapor and dry constituents, respectively;  $k_1$ ,  
 133  $k_2$  and  $k_3$  are the "Rueger - best average" values, which are 77.6890 K/hPa, 71.2952 K/hPa and  
 134 375463 K<sup>2</sup>/hPa respectively. In Eq. (5), all variables are constants except for the weighted average  
 135 temperature  $T_m$ .  $T_m$  is defined as:

$$136 \quad T_m = \frac{\int_{H_s}^{\infty} \left(\frac{e}{T}\right) dz}{\int_{H_s}^{\infty} \left(\frac{e}{T^2}\right) dz} = \frac{\sum_{H_s}^{H_{top}} \frac{e_j}{T_j} \Delta H_j}{\sum_{H_s}^{H_{top}} \frac{e_j}{T_j^2} \Delta H_j}, \quad (6)$$

137 where  $e$  and  $T$  are water vapor pressure (in hPa) and temperature (in K) profiles from station  
 138 height  $H_s$  to the top of the troposphere. Similar to ZHD computation, the Bevis model (*Bevis et al.*,  
 139 1992) is commonly employed for  $T_m$ 's calculation due to the difficulty in obtaining vertical profiles  
 140 of temperature and vapor pressure. This empirical model offers a practical alternative when detailed

141 atmospheric data is scarce.

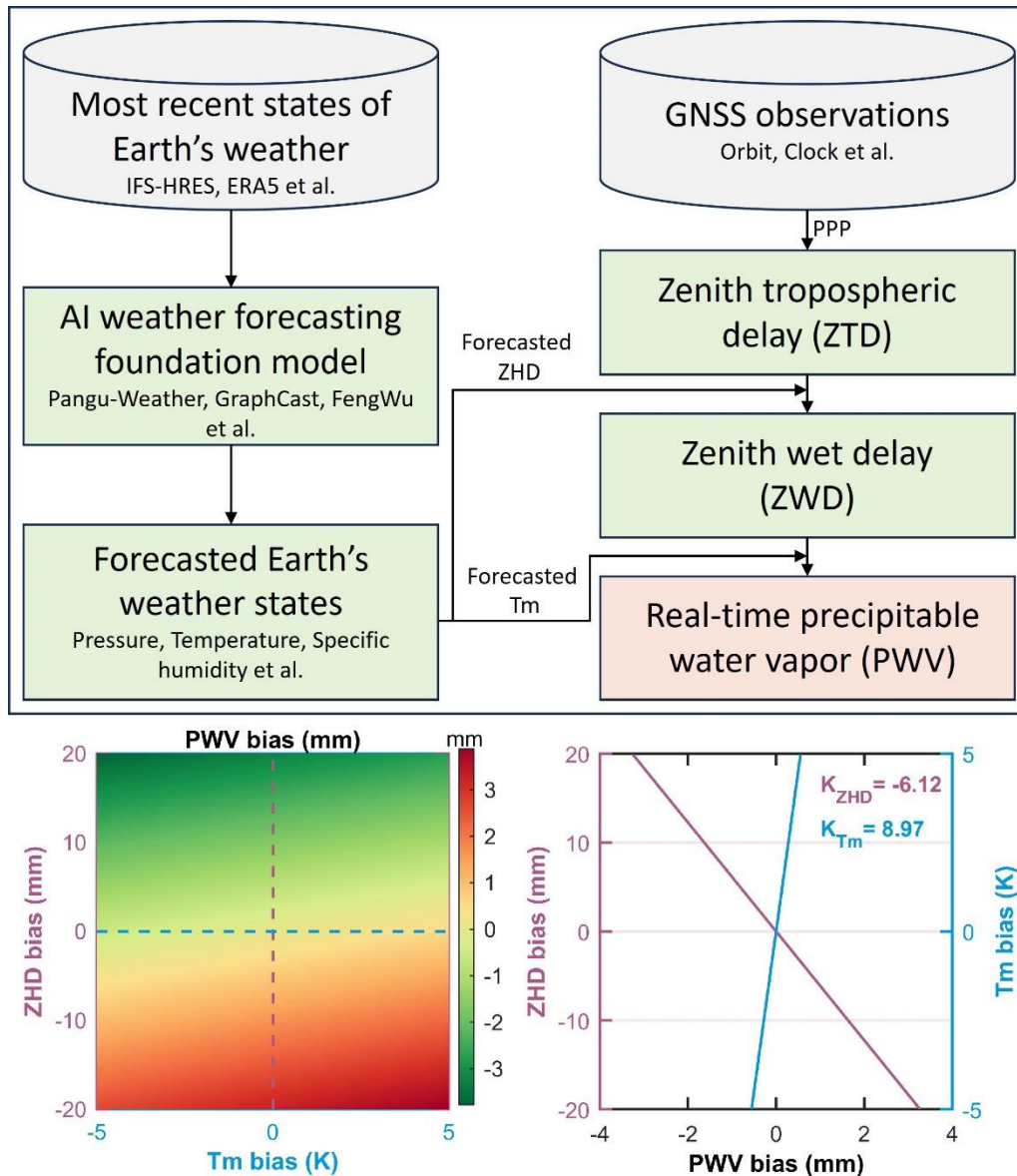
$$142 \quad T_m = 70.2 + 0.72 \cdot T_s \quad (7)$$

143 where  $T_s$  is the surface temperature at the site location. Note that in the integration method mentioned  
 144 above (Eq. 2 and Eq. 6), the top of the tropopause does not correspond to the topmost pressure level  
 145 of the NWM model (i.e. 1 hPa for ERA5). Instead, a reasonable extrapolation is performed as described  
 146 in *Hofmeister, 2016* for relevant vertical and horizontal interpolation methods. Note the empirical  
 147 models mentioned in this paper refer to the Saastamoinen and Bevis models (Eq. 3 and Eq. 7).

148

## 149 **2.2. AI Weather Forecast Foundation Models**

150 Pangu-Weather, developed by Huawei Cloud, is the first AI weather forecast foundation model to  
 151 exceed the accuracy of traditional numerical forecasting methods (operational IFS) for medium- and  
 152 long-term weather forecasts (*Bi et al., 2023*). It is constructed based on a 3D Earth-Specific  
 153 Transformer (3DEST), which can handle complex 3D meteorological data well and reduce iteration  
 154 error (*Bi et al., 2023*). GraphCast, proposed by Google DeepMind, is a state-of-the-art (SOTA) weather  
 155 forecasting foundation model based on graph neural networks (GNN) technology. Its "encode-process-  
 156 decode" modeling structure exhibits excellent performance, outperforming Pangu-Weather on 99.2%  
 157 of its targets (*Lam et al., 2023*). FengWu, proposed by the Shanghai Artificial Intelligence Laboratory,  
 158 is another advanced weather forecast foundation model. FengWu is based on multi-modal and multi-  
 159 task deep learning methods and performs better than GraphCast in predicting 80% of the 880 reported  
 160 predictands (*Chen et al., 2023*). Pangu-Weather and GraphCast are online as part of ECMWF's  
 161 operational suite, and everyone can benefit from their 10-day global weather forecasts without running  
 162 code. Note that Pangu-Weather only supports 13 layers of pressure level inference, while GraphCast  
 163 and FengWu support up to 37 layers. The foundation models employ a "roll back" method of  
 164 forecasting, wherein the input to each forecast is the output of its previous forecast. We employ a  
 165 minimum forecasting step of 6 hours in this experiment, and every forecast time is a multiple of 6  
 166 hours. As of March 2024, additional AI models like ClimaX, CliMA, FuXi, FourCastNet, and AIFS  
 167 have emerged; however, none support 37-layer pressure level inputs and some of them lack open access,  
 168 thus excluding them from this research framework.



169

170 **Figure 1.** Flowchart of real-time GNSS PWV retrieval system based on AI weather forecasting  
 171 foundation models and PWV bias caused by ZHD bias and Tm bias. The bottom right panel shows the  
 172 variation of PWV bias with the variation of Tm bias and ZHD bias for ZHD = 0 and Tm = 0, i.e., the  
 173 dashed line corresponding to the bottom left panel.

174

175 The upper panel of Figure 1 shows the technical flowchart of the proposed real-time GNSS PWV  
 176 retrieval strategy. The key is to obtain the forecasted ZHD and Tm from the AI foundation models. It  
 177 meets the needs of converting real-time GNSS tropospheric delays into real-time PWV while avoiding  
 178 errors introduced by empirical models. The lower panels of Figure 1 show the bias in PWV caused by  
 179 errors in ZHD and Tm according to Eqs. (1), (4) and (5). The results indicate that a  $\pm 6.12$  mm ZHD

180 bias or an  $\pm 8.97$  K Tm bias each leads to a 1 mm PWV bias.

181

### 182 **2.3. IGRA2 Radiosonde Data and NGL GNSS Tropospheric Products**

183 Global radiosonde observations from 2022 were utilized as a reference to assess the accuracy of the  
184 GNSS PWV under the proposed solution. The radiosonde observations were obtained from the  
185 Integrated Global Radiosonde Archive Version 2.2 (*Durre et al., 2018*). We applied stringent quality  
186 control to the dataset using the same strategy as *Zhang et al (2019)*, *Zheng et al. (2022)* and *Yuan et al*  
187 *(2023)*, i.e., (1) records are available at the surface and the top pressure level recorded is at least 300  
188 hPa; (2) there are at least five records of standard pressure levels below (and above) the pressure level  
189 of 1000 hPa; and (3) the gap between pressure levels is less than 200 hPa. Given the scarcity of stations  
190 in the dataset that fulfill all criteria, experiments included those stations with surface-level data records,  
191 enabling the empirical calculation of ZHD and Tm. However, it's important to note that this approach  
192 introduces errors from empirical modeling. To investigate this error, we designed experiments and then  
193 analyzed them in detail in Section 3.1.

194 The Nevada Geodetic Laboratory (NGL) provides tropospheric delay products from over 20,000  
195 GNSS stations worldwide, making it the most complete data set of tropospheric delays in the world  
196 today. The dataset spans the period from 1994 to the present and provides ZTD, ZWD, gradients and  
197 PWV in 5-minute interval. The accuracy of the NGL tropospheric products is comparable to that of  
198 the IGS products, making them a reliable reference for evaluating general tropospheric models (*Ding*  
199 *and Chen, 2020*). Note that the NGL strategy uses TU Wien's grid model for ZHD and Tm, which also  
200 causes NGL's ZWD and PWV products to include this model error (*Yuan et al., 2021; Ding et al.,*  
201 *2023*). Only NGL's ZTD product is used in our experiments.

202 As a special note, NGL ZTD is not designed for real-time applications. We selected it for our  
203 experiments because our goal is to establish a globally available method for converting GNSS ZTD to  
204 high-accuracy PWV in real-time, rather than providing the real-time GNSS PWV products. Therefore,  
205 the real-time nature of ZTD does not impact the conclusions drawn in this research. The accuracies  
206 mentioned in this research are also relative to those that would be achieved if ERA5 were used for  
207 retrospective calculations, representing relative accuracy. Additionally, users can also utilize the  
208 forecasted ZHD at the time of GNSS processing (we also recommend that); as the ZHD error will be  
209 absorbed by ZWD and have minimal impact on ZTD (*Ding et al., 2023*), this method is essentially

210 equivalent to the one depicted in Figure 1 of this paper.

211

### 212 **3. Results and Discussion**

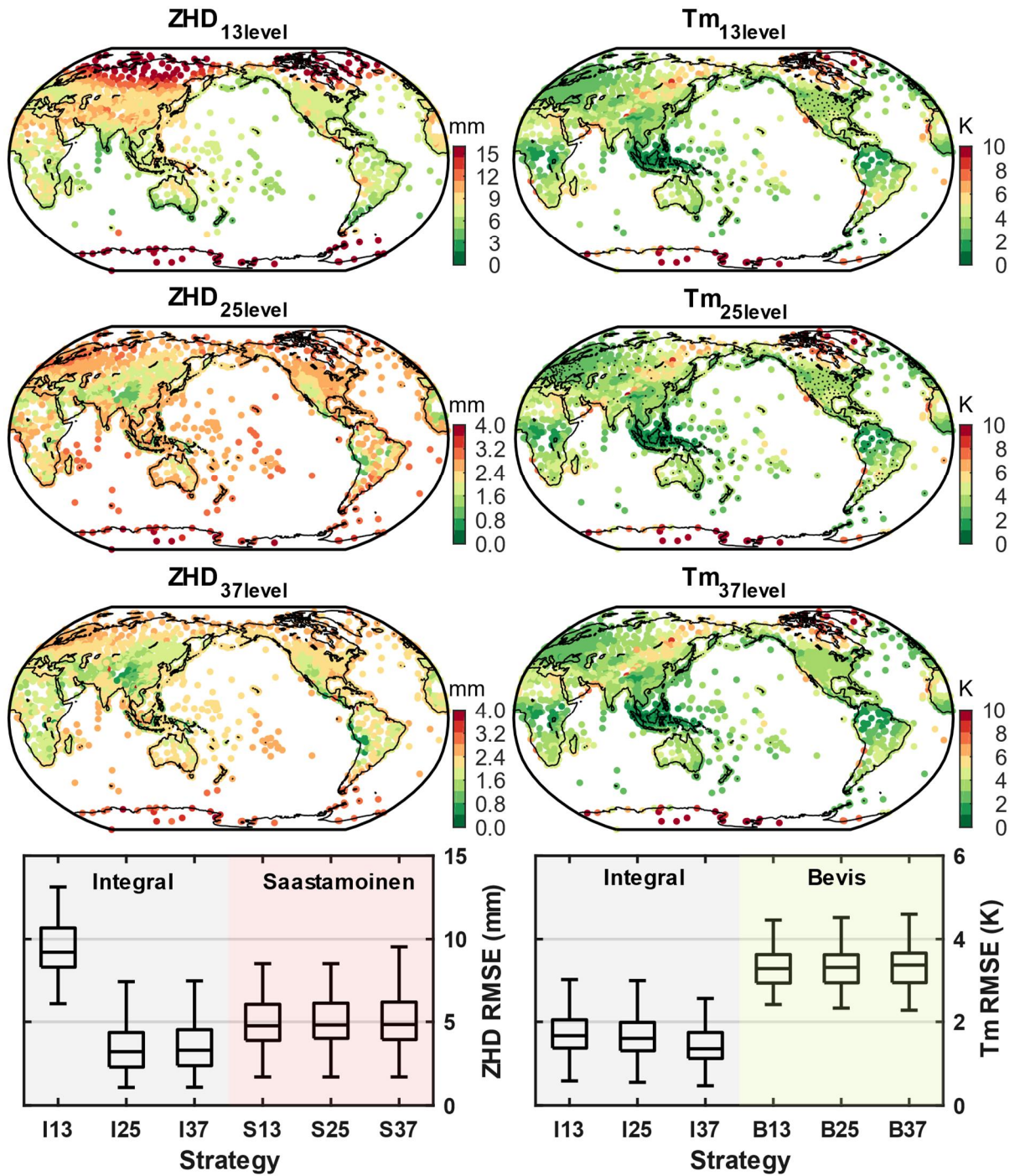
213 In this section, the accuracies of ZHD and  $T_m$  computed by the integral method and empirical models  
214 at different pressure levels are analyzed first. Then, the RMSEs of ZHD,  $T_m$ , and GNSS PWV for the  
215 three AI foundation models are obtained and analyzed for the 0-15 day forecast time horizon using  
216 ERA5 and co-location radiosonde measurements as references. Finally, the spatial characterization of  
217 the accuracy of the global GNSS PWV computed using the three AI foundation models is analyzed.

#### 218 **3.1. Vertical integrals vs. empirical models**

219 The upper panels of Figure 2 (scatter plots) display the RMSEs for ZHD and  $T_m$  at over 2,600  
220 radiosonde sites worldwide, derived from empirical models using 13-, 25-, and 37-level ERA5 data,  
221 with results from the integral method as reference. We specifically compare the 25-level results here  
222 because the VMF forecast products provided by TU Wien, which are based on the 25-level ECMWF  
223 products, include ZHD forecasts. It's important to note that VMF lacks  $T_m$  data for our study's  
224 experiments and its forecasted products can only be used to access previous years' data, with real-time  
225 results requiring licensing. The scatter plots in Figure 2 reveal that the ZHD RMSE at 13 pressure  
226 levels is notably higher compared to those at 25 and 37 pressure levels. However, the  $T_m$  results at 13  
227 pressure levels do not exhibit inferior performance relative to the results of the other two solutions.  
228 This is due to the fact that most of the missing pressure levels when using 13 levels are above 50 hPa,  
229 where there is almost no water vapor present, resulting in minimal contribution to the calculation of  
230  $T_m$ . For ZHD, the error due to the empirical model Saastamoinen is less than 3 mm for the majority  
231 of sites when using 25 level or 37 level. Similarly, for  $T_m$ , the error due to the empirical Bevis model  
232 is less than 4 K for the majority of sites, whether using 13, 25, or 37 levels. Note that in the polar  
233 region, it is not recommended to use the Bevis model as it may lead to errors exceeding 10 K.

234 The lower panels of Figure 2 (box plots) show the results of each solution using the radiosonde  
235 observations as a reference. There are only 93 stations that satisfy our requirements for the integration  
236 method, most of which are located in the United States (see the small black dots in the  $T_{m13level}$  plot in  
237 Figure 2). From the figure, we find that the integration method for the 13-level case yields a ZHD error  
238 of about 9 mm, which introducing an error larger than 1 mm to PWV, making it unacceptable.  
239 Therefore, we use Saastamoinen to calculate the ZHD under the Pangu-Weather solution in the

240 subsequent experiments. For the other pressure level configurations, the RMSEs of the integral method  
 241 achieve RMSE values of around 3 mm, while the Saastamoinen methods are all around 5 mm. The  
 242 difference in  $T_m$  between different pressure levels is minimal, with the RMSEs of the integral method  
 243 are all around 1.6 K, while the RMSEs of the Bevis method are all around 3.5 K. According to the  
 244 conversion relationship demonstrated in Figure 1, the empirical Saastamoinen model leads to a PWV  
 245 bias of about 0.3 mm, while the empirical Bevis model leads to a PWV bias of about 0.2 mm.



246

247 **Figure 2.** Root-mean-square errors (RMSEs) of zenith hydrostatic delay (ZHD) and weighted mean  
 248 temperature ( $T_m$ ) for different strategies (Integral vs. Saastamoinen for ZHD, Integral vs. Bevis for  
 249  $T_m$ ) using ERA5 of 13-, 25-, and 37- pressure levels. The global scatterplots show the comparison  
 250 between the integral method and the empirical model (Saastamoinen and Bevis), and the box plots  
 251 show the RMSE of the various strategies using the measured radiosonde data as a reference.

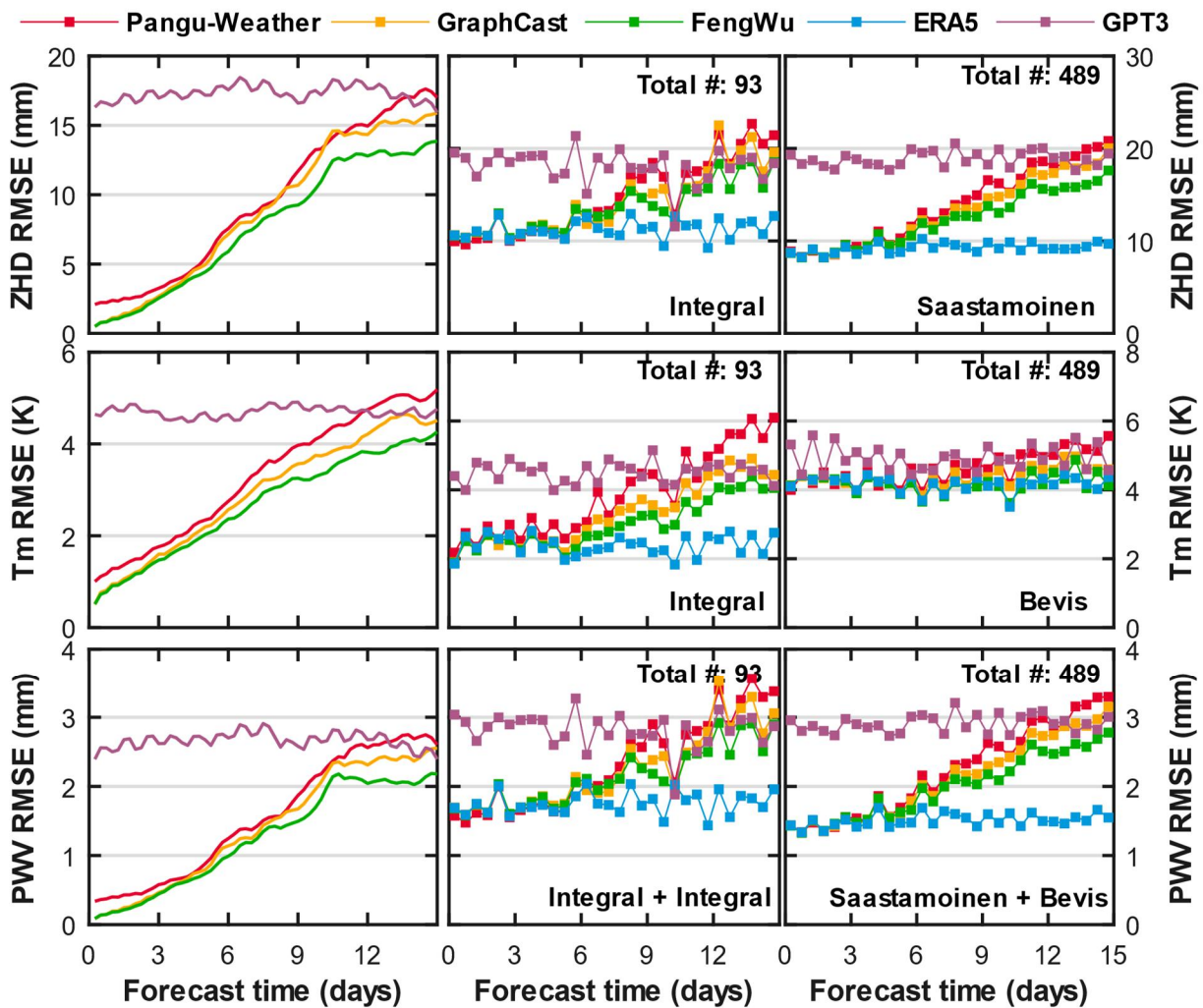
252

### 253 3.2. Accuracy Evaluation

254 Figure 3 shows the RMSE of ZHD,  $T_m$  and GNSS PWV calculated using the 0-15 day forecast results  
 255 from the Pangu-Weather, GraphCast and FengWu models. The left panels in Figure 3 depict the results  
 256 of the three AI foundation models for more than 8000 GNSS stations (see Figure 4 for individual  
 257 stations) using ERA5 as a reference, while the middle panels and the right panels are the results using  
 258 the co-located radiosonde data as a reference. Note that since there is no perfect (i.e., zero distance)  
 259 co-located, we define co-location as GNSS stations and radiosondes within 40 km. *Ding and Chen*  
 260 (2021) discuss the differences between the two sources of PWV as a function of distance, and we  
 261 follow their definition of co-location. The middle panels are the results for the 93 radiosonde stations  
 262 that are able to fulfill the requirements of the integration method, and the right panels are the results  
 263 for the 489 radiosonde stations (see the small black dots in the  $T_{m25level}$  plot in Figure 2) for which the  
 264 surface data records of the radiosonde stations are valid. Since the integration method cannot be used  
 265 at these locations, we rely on the empirical model to compute ZHD and  $T_m$ . Note that we included the  
 266 results using the empirical meteorological parameter model GPT3 (*Landskron & Böhm, 2018*) in the  
 267 comparison as well to have an intuitive reference for the degradation of the accuracy of the AI  
 268 foundation models with the forecast duration. Note that this empirical model is usually not used to  
 269 compute the PWVs because of its poor accuracy. If the method of *Zheng et al. (2022)* is applied to this  
 270 experiment, it is expected to perform similarly to the GPT3 model shown in Figure 3, essentially  
 271 resembling a horizontal straight line. Of course, its RMSE would be slightly lower than that of GPT3,  
 272 improving from 2.8 mm to 2.4 mm.

273 Pangu-Weather results in a significantly worse GNSS PWV accuracy than GraphCast and  
 274 FengWu because of fewer pressure level layers. The left panels in Figure 3 show that, the PWV error  
 275 introduced by the AI model error is less than 1 mm for forecasts less than five days ahead. From the  
 276 middle panels and right panels, we conclude that the PWVs calculated using the results from forecasts

277 shorter than three days are not significantly different under the three AI solutions as well as the ERA5  
 278 solution. In addition, in all comparisons, the results of forecasts up to 10 days are better than those of  
 279 the empirical model GPT3. Finally, we find that the trends of ZHD RMSE and PWV RMSE are very  
 280 similar in all comparisons because the ZHD error is the primary contributor to the PWV RMSE. The  
 281 Tm accuracy is generally very high and results in a smaller impact on the PWV RMSE. Combined  
 282 with the relationship from Figure 1, the contributions of ZHD and Tm are about 80% and 20%,  
 283 respectively.



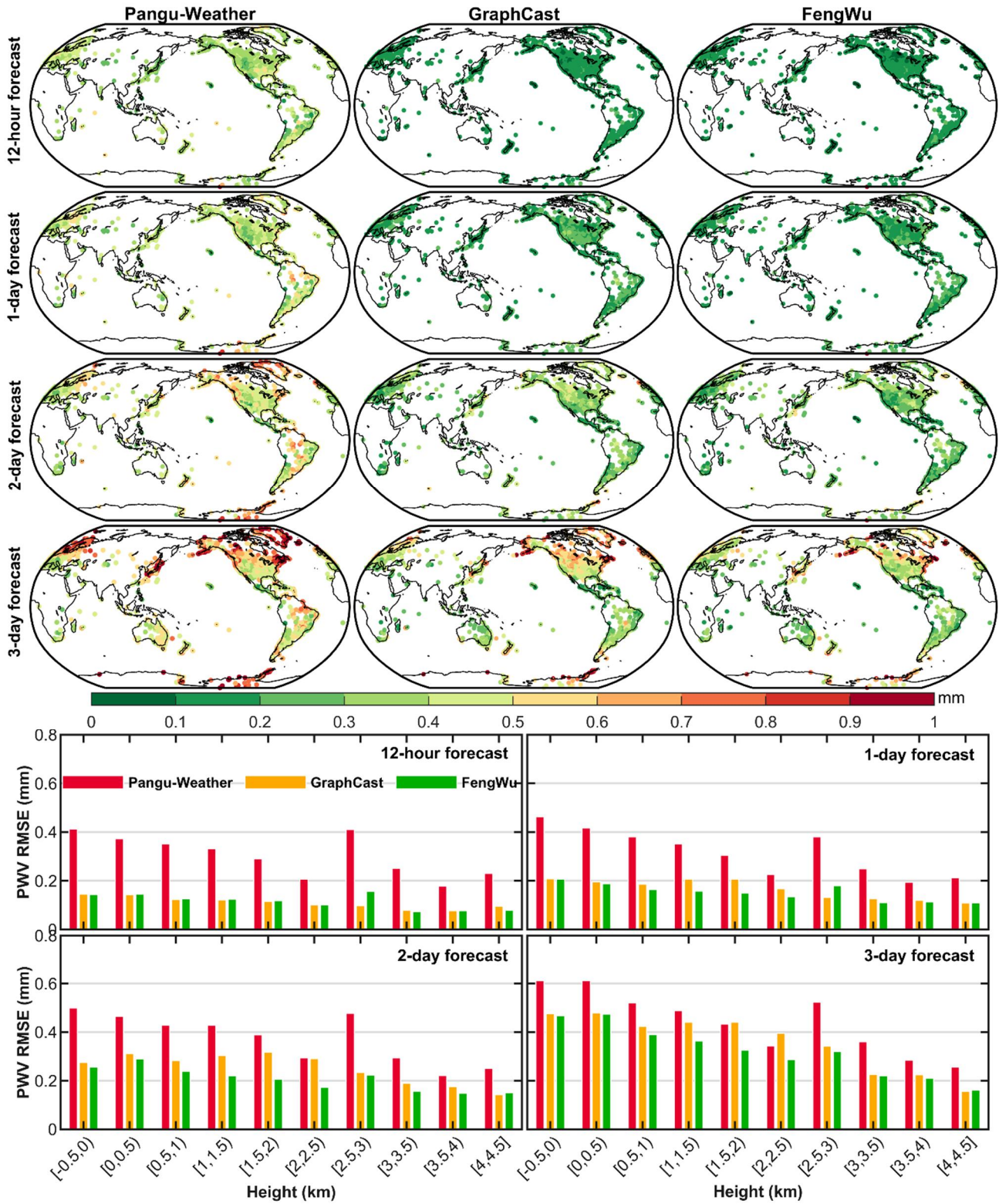
284  
 285 **Figure 3.** Variation of root-mean-square errors (RMSEs) with forecast time for ZHD, Tm and GNSS  
 286 PWV. The left panels are the RMSEs referenced to ERA5, and the middle and right panels are the  
 287 RMSEs referenced to co-located radiosonde observations. Note that all PWVs in the figure are all from  
 288 GNSS ZTD, and the only differences between the solutions are in the data sources for ZHD and Tm,  
 289 and in their calculation methods.

290

291 **3.3. Global GNSS PWV**

292 Based on the results in Figure 3 when using the radiosonde data as a reference, the accuracy of the  
293 GNSS PWV computed using the ZHD and  $T_m$  within 3 days of the forecast shows very little difference  
294 between the three AI solutions, and the difference is barely discernible from the results of using ERA5  
295 Figure 4 shows the RMSEs of 8320 stations for which the NGL GNSS ZTD data record meets the  
296 requirements, with forecast durations of 12 hours, 1 day, 2 days, and 3 days, respectively. The upper  
297 panels in Figure 4 show the RMSEs for each station, while the lower panels show the average RMSEs  
298 at 500 m intervals for different station height intervals. Note that the RMSEs here are calculated using  
299 the ERA5 results as a reference, i.e., the same strategy as the left panels in Figure 3.

300 Among the three AI solutions, GraphCast and FengWu are significantly ahead of Pangu-Weather,  
301 while FengWu slightly outperforms GraphCast for all forecast durations. There are two reasons for  
302 this result: firstly, Pangu-Weather only supports a maximum of 13 layers of pressure level, which is  
303 disadvantageous for accurately expressing the atmospheric state; secondly, the Pangu-Weather solution  
304 can only use the empirical model Saastamoinen to calculate the ZHD due to the large error in the  
305 integration method for the insufficient number of layers, and this part of the model error is introduced  
306 into the calculated PWV. The GNSS PWV accuracies degrade faster in the high-latitude region as the  
307 forecast duration increases. Moreover, the GNSS PWV accuracies degrade faster at the edge of  
308 continents, especially in narrow peninsulas or archipelagic regions, such as the Antarctic Peninsula,  
309 the Aleutian Islands, and the Newfoundland Islands region of Canada, among others. The former  
310 may be caused by the lower accuracy of ZHD in high latitude regions, while the latter may be caused  
311 by the sharp fluctuation of water vapor and the decrease in the accuracy of  $T_m$ . In terms of the change  
312 of PWV RMSE with height, overall, the PWV accuracy becomes higher with increasing station height,  
313 which is because the value of PWV itself also decreases with increasing height. In addition, the  
314 difference between the results of Pangu-Weather and the other two solutions becomes smaller as the  
315 forecast length increases, as well as the height increases. In contrast, the difference between the results  
316 of GraphCast and FengWu solutions is gets larger as the height increases.



317  
 318 **Figure 4.** Root-mean-square errors (RMSEs) of global GNSS PWV derived from three AI foundation  
 319 models w.r.t. to GNSS PWV using ERA5. The upper panels show the RMSEs of global GNSS sites  
 320 for 12-hour, 1-day, 2-day, and 3-day forecasts for the three solutions, respectively. The lower panels  
 321 show the RMSEs according to height partitioning under the same forecast durations.

322

#### 323 **4. Conclusions**

324 We presented a novel method to retrieve highly accurate real-time PWV from GNSS tropospheric  
325 delay based on AI weather forecast foundation models. In this method, the forecasted atmospheric state  
326 is firstly obtained by using foundation models such as Pangu-Weather, GraphCast, and FengWu, then  
327 the integral ZHD and integral Tm are computed from the forecasted atmospheric state, and finally, the  
328 high-precision real-time GNSS PWV is obtained from the real-time GNSS ZTD. Compared to  
329 conventional approaches, our method boasts three key benefits: (1) It enables the creation of pressure  
330 level atmospheric states at any global location directly on the user's computing device, thereby meeting  
331 the need for instantaneous PWV retrieval within seconds; (2) The atmospheric state produced is  
332 compatible with the integral method for calculating ZHD and Tm, circumventing the inaccuracies  
333 associated with empirical models (the compounded error from two empirical models could lead to a  
334 PWV RMSE of up to 0.5 mm); (3) This method ensures that the real-time GNSS PWV as close as  
335 possible to the results obtained through post-processing with reanalyzed NWM, thereby avoiding the  
336 inaccuracies introduced by varying spatial distances and the use of imperfectly co-located radiosonde  
337 observations. Of the three AI solutions, FengWu performs the best, followed by GraphCast, both of  
338 which are substantially ahead of Pangu-Weather. The PWV errors due to ZHD and Tm calculated using  
339 forecasts shorter than 3 days are not significantly different from the post-processed PWV errors  
340 calculated using ERA5 results. The PWV errors introduced by the AI-based forecasts are typically less  
341 than 1 mm when calculated using forecasts less than 5 days ahead.

342 The proposed method has the potential to significantly contribute to atmospheric monitoring  
343 significantly by providing high-accuracy forecasted ZHD and Tm for real-time GNSS PWV retrieval  
344 at any global position within seconds, ensuring a precision loss of GNSS PWV within 0.1 mm (6-hour  
345 forecast) due to incorrect ZHD and Tm. This will enable the global network of dense GNSS stations  
346 to offer reliable and timely PWV for weather disaster prediction and alerts. We recommend substituting  
347 the traditional GNSS PWV retrieval from ZTD with this novel method to preserve GNSS technology's  
348 edge in delivering real-time products with minimal accuracy degradation. It is crucial to emphasize the  
349 significance of utilizing a highly accurate NWM for the initial epoch inference of the AI forecast model,  
350 as employing a lower accuracy NWM could result in cumulative errors in the final PWV.

351

## 352 **Data Availability Statement**

353 This research processed data from more than 20 TB. The ERA5 data on pressure levels (*Hersbach et al., 2018a*) and ERA5 data on single levels (*Hersbach et al., 2018b*) are available at Copernicus  
 354 Climate Change Service (C3S) Climate Data Store (CDS) (last accessed 8 Oct, 2023). The NGL GNSS  
 355 tropospheric delay products are available at [http://geodesy.unr.edu/gps\\_timeseries/trop/](http://geodesy.unr.edu/gps_timeseries/trop/) (*Blewitt et al.,*  
 356 *2018*). The radiosonde data is available at [https://www.ncei.noaa.gov/products/weather-](https://www.ncei.noaa.gov/products/weather-balloon/integrated-global-radiosonde-archive)  
 357 [balloon/integrated-global-radiosonde-archive](https://www.ncei.noaa.gov/products/weather-balloon/integrated-global-radiosonde-archive) (*Durre et al., 2018*). The foundation model Pangu-  
 358 Weather is available at <https://github.com/198808xc/Pangu-Weather> (*Bi et al., 2023*). The foundation  
 359 model GraphCast is available at <https://github.com/google-deepmind/graphcast> (*Lam et al., 2023*). The  
 360 foundation model FengWu is available at <https://github.com/OpenEarthLab/FengWu> (*Chen et al.,*  
 361 *2023*).  
 362

363

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## 373 **References**

- 374 Adams, D. K., Gutman, S. I., Holub, K. L., & Pereira, D. S. (2013). GNSS observations of deep  
 375 convective time scales in the Amazon. *Geophysical Research Letters*, 40(11), 2818-2823.  
 376 <https://doi.org/10.1002/grl.50573>
- 377 Bevis, M., Businger, S., Herring, T. A., Rocken, C., Anthes, R. A., & Ware, R. H. (1992). GPS  
 378 meteorology: Remote sensing of atmospheric water vapor using the global positioning system.  
 379 *Journal of Geophysical Research: Atmospheres*, 97(D14), 15787-15801.  
 380 <https://doi.org/10.1029/92JD01517>
- 381 Bi, K., Xie, L., Zhang, H., Chen, X., Gu, X., & Tian, Q. (2023). Accurate medium-range global weather

- 382 forecasting with 3D neural networks. *Nature*, 619(7970), 533-538.  
383 <https://doi.org/10.1038/s41586-023-06185-3>
- 384 Blewitt, G., & Hammond, W. (2018). Harnessing the GPS data explosion for interdisciplinary science.  
385 *Eos*, 99. <https://doi.org/10.1029/2018EO104623>
- 386 Chen, K., Han, T., Gong, J., Bai, L., Ling, F., Luo, J. J., ... & Ouyang, W. (2023). FengWu: Pushing  
387 the Skillful Global Medium-range Weather Forecast beyond 10 Days Lead. *arXiv preprint*  
388 *arXiv:2304.02948*. <https://doi.org/10.48550/arXiv.2304.02948>
- 389 Ding, J., & Chen, J. (2020). Assessment of empirical troposphere model GPT3 based on NGL's global  
390 troposphere products. *Sensors*, 20(13), 3631. <https://doi.org/10.3390/s20133631>
- 391 Ding, J., & Chen, J. (2021). Accuracy Variability of GNSS PWV in the Range of Small and Medium  
392 Scale Areas. *Proceedings of the 12th Annual China Satellite Navigation Conference - S01*  
393 *Satellite Navigation Industry Applications*.
- 394 Ding, J., Chen, J., Tang, W., & Song, Z. (2022a). Spatial–Temporal Variability of Global GNSS-  
395 Derived Precipitable Water Vapor (1994–2020) and Climate Implications. *Remote Sensing*,  
396 14(14), 3493. <https://doi.org/10.3390/rs14143493>
- 397 Ding, J., Chen, J., & Tang, W. (2022b). Increasing Trend of Precipitable Water Vapor in Antarctica and  
398 Greenland. In *China Satellite Navigation Conference (pp. 286-296)*. Singapore: Springer Nature  
399 Singapore. [https://doi.org/10.1007/978-981-19-2588-7\\_27](https://doi.org/10.1007/978-981-19-2588-7_27)
- 400 Ding, J., Chen, J., Wang, J., & Zhang, Y. (2023). Characteristic differences in tropospheric delay  
401 between Nevada Geodetic Laboratory products and NWM ray-tracing. *GPS Solutions*, 27(1), 47.  
402 <https://doi.org/10.1007/s10291-022-01385-2>
- 403 Ding, W., Teferle, F. N., Kazmierski, K., Laurichesse, D., & Yuan, Y. (2017). An evaluation of real-  
404 time troposphere estimation based on GNSS Precise Point Positioning. *Journal of Geophysical*  
405 *Research: Atmospheres*, 122(5), 2779-2790. <https://doi.org/10.1002/2016JD025727>
- 406 Durre, I., Yin, X., Vose, R. S., Applequist, S., & Arnfield, J. (2018). Enhancing the data coverage in  
407 the Integrated Global Radiosonde Archive. *Journal of Atmospheric and Oceanic Technology*,  
408 35(9), 1753-1770. <https://doi.org/10.1175/JTECH-D-17-0223.1>
- 409 Ejigu, Y. G., Teferle, F. N., Klos, A., Bogusz, J., & Hunegnaw, A. (2021). Monitoring and prediction  
410 of hurricane tracks using GPS tropospheric products. *GPS Solutions*, 25(2), 76.  
411 <https://doi.org/10.1007/s10291-021-01104-3>

- 412 Guo, A., Xu, Y., Jiang, N., Wu, Y., Gao, Z., Li, S., ... & Bastos, L. (2023). Analyzing correlations  
413 between GNSS retrieved precipitable water vapor and land surface temperature after earthquakes  
414 occurrence. *Science of The Total Environment*, 872, 162225.  
415 <https://doi.org/10.1016/j.scitotenv.2023.162225>
- 416 Hersbach, H., Bell, B., Berrisford, P., Biavati, G., Horányi, A., Muñoz Sabater, J., ... & Thépaut, J. N.  
417 (2018a). ERA5 hourly data on pressure levels from 1979 to present. *Copernicus climate change*  
418 *service (c3s) climate data store (cds)*, 10(10.24381). doi: 10.24381/cds.bd0915c6.
- 419 Hersbach, H., Bell, B., Berrisford, P., Biavati, G., Horányi, A., Muñoz Sabater, J., ... & Thépaut, J. N.  
420 (2018b). ERA5 hourly data on single levels from 1979 to present. *Copernicus climate change*  
421 *service (c3s) climate data store (cds)*, 10(10.24381). doi: 10.24381/cds.adbb2d47.
- 422 Hofmeister, A. (2016). Determination of path delays in the atmosphere for geodetic VLBI by means  
423 of ray-tracing. <http://hdl.handle.net/20.500.12708/136>
- 424 Huang, L., Mo, Z., Xie, S., Liu, L., Chen, J., Kang, C., & Wang, S. (2021). Spatiotemporal  
425 characteristics of GNSS-derived precipitable water vapor during heavy rainfall events in Guilin,  
426 China. *Satellite Navigation*, 2, 1-17. <https://doi.org/10.1186/s43020-021-00046-y>
- 427 Jade, S., & Vijayan, M. S. M. (2008). GPS-based atmospheric precipitable water vapor estimation  
428 using meteorological parameters interpolated from NCEP global reanalysis data. *Journal of*  
429 *Geophysical Research: Atmospheres*, 113(D3). <https://doi.org/10.1029/2007JD008758>
- 430 Jiang, N., Wu, Y., Li, S., Xu, Y., Wang, Y., & Xu, T. (2024). First PWV retrieval using MERSI-LL  
431 onboard FY-3E and cross validation with co-platform occultation and ground GNSS. *Geophysical*  
432 *Research Letters*, 51(8), e2024GL108681. <https://doi.org/10.1029/2024GL108681>
- 433 Lam, R., Sanchez-Gonzalez, A., Willson, M., Wirnsberger, P., Fortunato, M., Alet, F., ... & Battaglia,  
434 P. (2023). Learning skillful medium-range global weather forecasting. *Science*, eadi2336.  
435 <https://doi.org/10.1126/science.adi2336>
- 436 Landskron, D., & Böhm, J. (2018). VMF3/GPT3: refined discrete and empirical troposphere mapping  
437 functions. *Journal of Geodesy*, 92, 349-360. <https://doi.org/10.1007/s00190-017-1066-2>
- 438 Li, X., Tan, H., Li, X., Dick, G., Wickert, J., & Schuh, H. (2018). Real-Time Sensing of Precipitable  
439 Water Vapor from BeiDou Observations: Hong Kong and CMONOC Networks. *Journal of*  
440 *Geophysical Research: Atmospheres*, 123(15), 7897-7909.  
441 <https://doi.org/10.1029/2018JD028320>

- 442 Ma, X., Yao, Y., Zhang, B., & He, C. (2022). Retrieval of high spatial resolution precipitable water  
443 vapor maps using heterogeneous earth observation data. *Remote Sensing of Environment*, 278,  
444 113100. <https://doi.org/10.1016/j.rse.2022.113100>
- 445 Miranda, P. M. A., Adams, D. K., Tomé, R., Fernandes, R., & Mateus, P. (2023). Optimizing Boundary  
446 Conditions in GNSS Tomography: A Continuous 7-Month Case Study in the Amazon.  
447 *Geophysical Research Letters*, 50(22), e2023GL105030. <https://doi.org/10.1029/2023GL105030>
- 448 Rocken, C., Van Hove, T., & Ware, R. (1997). Near real-time GPS sensing of atmospheric water vapor.  
449 *Geophysical research letters*, 24(24), 3221-3224. <https://doi.org/10.1029/97GL03312>
- 450 Saastamoinen, J. (1972). Atmospheric correction for the troposphere and stratosphere in radio ranging  
451 satellites. *The use of Artificial Satellites for Geodesy*, 15, 247-251.  
452 <https://doi.org/10.1029/GM015p0247>
- 453 Vaquero-Martínez, J., Antón, M., de Galisteo, J. P. O., Román, R., Cachorro, V. E., & Mateos, D.  
454 (2019). Comparison of integrated water vapor from GNSS and radiosounding at four GRUAN  
455 stations. *Science of the total environment*, 648, 1639-1648.  
456 <https://doi.org/10.1016/j.scitotenv.2018.08.192>
- 457 Wang, J., Wu, Z., Semmling, M., Zus, F., Gerland, S., Ramatschi, M., ... & Schuh, H. (2019).  
458 Retrieving precipitable water vapor from shipborne multi-GNSS observations. *Geophysical*  
459 *Research Letters*, 46(9), 5000-5008. <https://doi.org/10.1029/2019GL082136>
- 460 Wang, J., Zhang, L., Dai, A., Van Hove, T., & Van Baelen, J. (2007). A near-global, 2-hourly data set  
461 of atmospheric precipitable water from ground-based GPS measurements. *Journal of Geophysical*  
462 *Research: Atmospheres*, 112(D11). <https://doi.org/10.1029/2006JD007529>
- 463 Wang, X., Zhang, K., Wu, S., Li, Z., Cheng, Y., Li, L., & Yuan, H. (2018). The correlation between  
464 GNSS-derived precipitable water vapor and sea surface temperature and its responses to El Niño–  
465 Southern Oscillation. *Remote sensing of environment*, 216, 1-12.  
466 <https://doi.org/10.1016/j.rse.2018.06.029>
- 467 Wei, J., Shu, Y., Liu, Y., Fang, R., Qiao, L., Ding, D., ... & Liu, J. (2023). Retrieving Accurate  
468 Precipitable Water Vapor Based on GNSS Multi-Antenna PPP With an Ocean-Based Dynamic  
469 Experiment. *Geophysical Research Letters*, 50(6), e2023GL102982.  
470 <https://doi.org/10.1029/2023GL102982>
- 471 Wu, Z., Lu, C., Han, X., Zheng, Y., Wang, B., Wang, J., ... & Liu, Y. (2023). Real-time shipborne multi-

- 472 GNSS atmospheric water vapor retrieval over the South China Sea. *GPS Solutions*, 27(4), 179.  
473 <https://doi.org/10.1007/s10291-023-01519-0>
- 474 Yu, C., Penna, N. T., & Li, Z. (2017). Generation of real-time mode high-resolution water vapor fields  
475 from GPS observations. *Journal of Geophysical Research: Atmospheres*, 122(3), 2008-2025.  
476 <https://doi.org/10.1002/2016JD025753>
- 477 Yuan, P., Blewitt, G., Kreemer, C., Hammond, W. C., Argus, D., Yin, X., ... & Kutterer, H. (2023). An  
478 enhanced integrated water vapour dataset from more than 10,000 global ground-based GPS  
479 stations in 2020. *Earth System Science Data*, 15, 723–743. [https://doi.org/10.5194/essd-15-723-](https://doi.org/10.5194/essd-15-723-2023)  
480 [2023](https://doi.org/10.5194/essd-15-723-2023)
- 481 Yuan, P., Hunegnaw, A., Alshawaf, F., Awange, J., Klos, A., Teferle, F. N., & Kutterer, H. (2021).  
482 Feasibility of ERA5 integrated water vapor trends for climate change analysis in continental  
483 Europe: An evaluation with GPS (1994–2019) by considering statistical significance. *Remote*  
484 *Sensing of Environment*, 260, 112416. <https://doi.org/10.1016/j.rse.2021.112416>
- 485 Yuan, Y., Zhang, K., Rohm, W., Choy, S., Norman, R., & Wang, C. S. (2014). Real-time retrieval of  
486 precipitable water vapor from GPS precise point positioning. *Journal of geophysical research:*  
487 *atmospheres*, 119(16), 10044-10057. <https://doi.org/10.1002/2014JD021486>
- 488 Zhao, Q., Liu, Y., Ma, X., Yao, W., Yao, Y., & Li, X. (2020). An improved rainfall forecasting model  
489 based on GNSS observations. *IEEE Transactions on Geoscience and Remote Sensing*, 58(7),  
490 4891-4900. <https://doi.org/10.1109/TGRS.2020.2968124>
- 491 Zhang, W., Lou, Y., Cao, Y., Liang, H., Shi, C., Huang, J., ... & Fan, B. (2019). Corrections of  
492 radiosonde-based precipitable water using ground-based GPS and applications on historical  
493 radiosonde data over China. *Journal of Geophysical Research: Atmospheres*, 124(6), 3208-3222.  
494 <https://doi.org/10.1029/2018JD029662>
- 495 Zheng, Y., Lu, C., Wu, Z., Liao, J., Zhang, Y., & Wang, Q. (2022). Machine Learning-Based Model for  
496 Real-Time GNSS Precipitable Water Vapor Sensing. *Geophysical Research Letters*, 49(3),  
497 e2021GL096408. <https://doi.org/10.1029/2021GL096408>
- 498 Zhu, H., Chen, K., Chai, H., Ye, Y., & Liu, W. (2024). Characterizing extreme drought and wetness in  
499 Guangdong, China using global navigation satellite system and precipitation data. *Satellite*  
500 *Navigation*, 5(1), 1. <https://doi.org/10.1186/s43020-023-00121-6>